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COUNTRY	East Germany/USSR		REPORT	
SUBJECT	Exterior Ballistics of the Rocket at Gema, Berlin, and	"Wasserfall" d Ostashkov	DATE DISTR. NO. OF PAGES 17	31 August 1953 25X1
DATE OF INFO.		·]	REQUIREMENT	. ·
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Symbol Designations and Formulation of the Equations of Metion to Calculate Election Trajectories, Gena, and Ostashkey (1945)

11.	To avoid repetitions the	following basic symbol	designations are here-
	With presented:		· 1. 1.

With presented:	
a (m/sec)	velocity of sound
A (kg)	lifting force
o (m/sec)	exhaust velocity of combustion gases
c _e (1)	lift coefficient
c_ (1)	resistance coefficient
d (m)	maximum diameter of the recket
• (m)	distance from the starting point on the earth surface
• ₁ (a)	distance of the pressure point (point of application of the listing force) from the ness of the rocket
g ₂ (m)	distance of the rudder-pressure-center from the none of the recket
• ₅ (m)	distance of the jet pressure point from the nose of the rocket
F (n ²)	maximum cross-section of the rocket
7 _D (n ²)	end cross-section of the laval nessle
g (1/800 ²)	accoloration of gravity
G (kg)	weight of the rocket
h (m)	altitude above the earth's surface
1 (m)	length of the rocket
m (kg sec ² /m)	mass of the rooket
Ma (1)	Mach number
n (1)	lead factor (lift:weight)
$p(kg/n^2)$	atmospheric pressure
P (kg/radian)	jet cross force per radian of the rudder deflection
$q (kg/n^2)$	dynamic pressure
r, (m)	distance of a trajectory point from the launching

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R	(m)	earth radius
8	(m)	distance of the center of gravity from the mose of the rocket
8	(kg)	thrust
ŧ	(sec)	time
T	(°K)	temperature
•	(m/sec)	velocity
W	(kg)	air resistance
x	(m)	herizental distance in the tangential plane, through the launching point
y	(m)	height ever the tangential plane through starting point
	(n)	third coordinate vertically through x and y
≪	(degrees)	angle of incidence between path tangent and the lengi- tudinal axis of the rocket
*	(degrees)	inclination angle of the flight path between x axis and path tangent
η	(degrees)	rudder angle
غه	(degrees)	angle between x axis and longitudinal axis of the rocket
μ	(1)	mass ratio
P	$(kg seo^2/n^4)$	air density
e	(degrees)	angle between vectors, center of the earth - launching point and center of the earth - path point of the recket (Notes in general equations the angles are taken in circular measure).

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12. The plane powered trajectory:

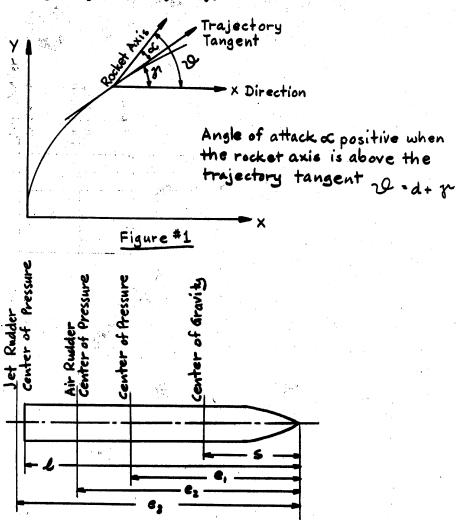


Figure #2

Meaning of the subscripts:

0= Value at the start (t=0) or on the ground (h=0)

= Value in a vacuum.

- 13. For the ballistic calculations the motion equations were formulated as fellews:
 - a. Force equation (in flight path direction):

 mv = 5-W-mg sin X
 - b. Force equation (perpendicular to path direction):
 - mv $\hat{y} = S\alpha + qF \frac{\partial C_{\alpha}}{\partial \alpha} \propto + qF \frac{\partial C_{\alpha}}{\partial \eta} \eta + P\eta mg$ Cos \hat{y} c. Moments equations
- $(e_1-s)qF\frac{\partial C_a}{\partial \alpha} \propto + (e_2-s)qF\frac{\partial C_a}{\partial \eta} \eta + (e_3-s)P\eta = 0$ 14. In the first equation appears, thrust, whereby the component
- 14. In the first equation appears thrust, whereby the component S cosoc is substituted by S, air resistance, and the weight component.
- 16. The thrust is composed of the thrust on the earth surface S, the thrust increase with altitude P,F,(I-P/P,), and if there are jet rudders, the thrust less through the jet rudders \$\Delta\$ S. For \$\Delta\$, a constant medium value was fixed independent of the rudder deflection.
- 16. Dr. WOLFF and Dr. ALBRING had established the mean value to use, probably by means of data from Peenemuende. AS was of the order of 12-15% of S for maximum rudder deflection of 25.
- 17. For the thrust the equation is: $S = S_0 + P_0 F_0 (1 P_0) \Delta S_0$ or also emphasizing the thrust in a vacuum (8 ∞) $S = S_0 P_0 F_0 \frac{P_0}{P_0} \Delta S_0$
- 18. The mass m is a linear function of the times mum, + mt whereby m is negative. m was generally calculated as constant. In several A-4 calculations a variable weight rate of flow for the first four seconds was calculated until the full thrust was achieved.
- 19. Ground thrust and thrust in a vacuum were formulated as follows: $S = |\dot{m}/C_o|$ and $S = |\dot{m}/C_o|$
- 20. Co and Coo were hereby exhaust speed of the gases on the ground and in a vacuum, respectively. Accordingly, altitude variable exhaust speed (o) was introduced by the relation S = /M/C.
- 21. The air resistance has the form: Wag Faw with q = \frac{2}{2} v2 = \frac{2}{2} \frac{2}{2} v2.
- number Mark. The altitude h and for antiaircraft rockets of the angle of incidence of the guided missiles the function of the angle of incidence was generally neglected for Eqt. (1) only.

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- a table existed, which used as basic data the values of the German artillery (normal atmosphere). For higher altitudes a temperature curve was taken, which Prof. SEELIGER (Greifswald) stated in a report which he wrote in 1945 for the Zentralwerke Bleicherode. The table covered an altitude up to 80 kilometers. Furthermore, the table centained the curve of g as a function of the altitude (g = 9.810 met/sec).
- 24. (Since about 1950 another table of the atmosphere was used, in which data on the ground values is given by Schapiro, a temperature curve in low altitudes is taken from Russian literature (Schapiro), and for high altitudes a curve derived from foreign experimental results () were used. The literature was available in the branch library. The researcher for this table of the atmosphere was Dr. SCHLIER. the new table covered up to 100 kilometers altitude. One of the reasons for making up a new table was that in the old table P/P, and P/P, were given to three valid places. This resulted in some cases by integrating in an irregular course of the differences. The new table was calculated for four valid places.)
- 25. In the second equation appears the thrust component, in which Sin a is replaced by at, the lift, the rudder forces and the weight component. In the lift coefficient scale as a function of the Mach number and eventually of the altitude, scale as a function of the Mach number was given. These values were given by acredynamics in such a form that the largest cross-section of the rocket was always taken as the datum plane. If the rocket had jet rudders, the resulting cross force was applied in form Pn with constant P.
- 26. In the moments equation, corresponding to the values in the second force equation, the factors of the factors of the factors of the points of application of these forces from the center of gravity are C.-S., C.-S., and C.-S. respectively. The curve of (s) a function of time (t), or of the recket mass was determined by the design section; the aerodynamics section supplied the curve of C. as a function of the Mach number; C. and C. are constant; C. was in general slightly larger than the length (1) of the recket. The data for center of gravity and pressure center curve were as usual without dimensions in the form 1, C. C.

 For the ballistic calculations in every instance moment balance was assumed, so that the right side of the equation (3) was equal to zero. Therefore it was not necessary for ballistics to know the moment of inertia around the transverse axis of the rocket; in first place the complicating factors 1 and 1 in the mathematical treatment of the equation system were eliminated (2 angle between rocket axis and horizontal plane).
- 27. For ballistic investigations no further factors were considered. The consideration of further moments and the process of stability examinations were the task of the guidance section (Dr. HOCH).

28. ROCH used his "Bahnmedell" for the study of the second force equation and the mements equation, and also for the examination of the side stability.

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- 29. In the above formulation the equations 2 and 3 represent linear equations for the angles of incidence and the rudder angle γ .
- 30. Equation (3) has the result:
 - (4) n = Kac

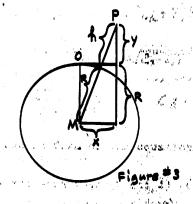
wi th

(5)
$$k = \frac{(e_1-s)q Fcd}{(e_2-s)q Fcd+(e_3-s)P}$$

- 31. The second form of the equation (5) arises, if no jet rudders are included (P = 0).
- 32. From the equations (2 and 4) results

with

- 33. The second form of the equation (7) is again for P=0.
- 34. To the equations (1) to (3) belong the equations for the trajectory coordinates:
 - (8) X . V Cos &
- 11. (9) 4 = V Sing
- 25. At smell distances from the launching point Y can be taken as altitudes (h) over the earth surface. At greater distances the difference between h and Y has to be considered:
 - (10) h= y+ Ah



- 0 = starting point (sero point of the x, y coordinate avetem)
- M = senter of the earth
- P = trajectory paint with coordinates x, y
- R = radius of the earth = 6370 kilometers

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- 36. From $(R+h)^2 = (R+y)^2 + x^2$
 - and (10) disregarding $(\Delta h)^{2}$: $(R+Y)^{2}+2(R+Y)\Delta h=(R+Y)^{2}+x^{2}$

or (11)
$$\Delta h = \frac{\chi^2}{2(R+Y)} = \frac{\chi^2}{2R} \left(\frac{1}{1+V/R} \right) \approx \frac{\chi^2}{2R} \left(1 - \frac{\chi}{R} \right)$$

- 37. For powered flight path the approximation (11') $\Delta h \approx \frac{\chi^2}{2R}$ is generally sufficient.
- 38. For Ah as a function of X or of X and Y, tables were established.
- 39. In connection with the curvature of the earth, which determines the difference between h and y, it must be said, that gravity for greater distance from the zero point of the coordinates system has a noticeable x-component. When in the sketch Figure No. 3 the angle at P, which is equal to the angle OMP, is designated as φ, the gravity component is: $q_{x} = -q \sin φ = -q \frac{x}{R+N} \approx -q \frac{x}{R}$

- 40. The consideration of g was done, if at all necessary, by a separate disturbance calculation. This was not done for the Wasserfall, but was considered for R-10, R-12, R-14 and V-2. Unknown factors in the equation (1) ares velocity v, altitude h, which appears in S, W and g, and the inclination angle of flight path & . Through altitude equation (1) is coupled with equation (9), and in case the difference between h and y has to be considered also with equation (8), so that these differential equations must be integrated simultaneously.
- 41. The whole equation system has one more unknown factor than the number of equations. This gives the liberty to assume one condition.
- 42. The possibilities are the fellowing:
 - a. The inclination angle of flight path & is prescribed,
 - b. The angle of incidence & is prescribed.
 - c. In anticircraft reckets: the altitude angle [, under which the rocket appears from the starting point, is prescribed. In this case also the connection between [and the other values is needed.
- 43. If 6 is prescribed, or fixed for other reasons, then equations (1), (8), (9), (11) represent four equations for the four unknown factors y, x, y, An. The first three equations of the above group are ordinary differential equations of first order.

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Procedure for Numerical Integration of Differential Equations

- 44. The first force equation and the equations for the trajectory coordinates with the starting conditions x = 0, y = 0 for \$\infty\$ were integrated in the Ballistics Section by Dr. WOLFF using the Bessel method. The reason was the followings in Bleicherede Dr. SCHLIER had worked with this system and the calculation personnel had learned it, because he had already used it in Psenemuende. Therefore, the use of this system was continued in Ostashkew and the eld personnel were not forced to learn a new method.
- 45. In the working group of Prof.KLOSE integration was done using the method of Adams-Steermer, probably because KLOSE was familiar with this method from experience in Germany.
- 46. The Soviet assistants who were assigned to us in Ostashkev (females with high school education) had no knowledge of the integration of differential equations, and were taught the Bessel method by us. They proved to be good calculators. Once, two computers came as help from Mescew. They used the Adams-Steermer system and told us that this system was always used.

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- 47. The integration of the equations (1), (8), (9) was done in general with the interval Δt = 2 sec. When Δ-4 trajectories were not inmediately calculated with full thrust, but with increase of the thrust up to full thrust, then Δt = 0.5 sec was selected in the first four to six seconds as an integration interval. But generally calculations were done with full thrust from the start.
- 48. Acceleration * was calculated to a hundredth of m/sec2, velocity v to a tenth of m/sec, coordinates were calculated to the nearest meter. Later the mass ratio was reften selected as an independent variable instead of the time t. This has several small advantages for the numerical calculations.

Activity at "Gene". Berlin (July to October 1946) -- Mainly Concerned with "Vasserfall" Missile

9.	Among the members of the group were a number	1
	of younger persons who had already worked during the war with Prof.	
	ELOSE in Engersderf, especially a Dipl. Phys. STANGE and a Dipl. Chem.	
•	KIUGE. Several technical calculators and draftsmen served as assis-	
	tants; there was also one stenotypist. The Soviet supervisors of the section were: Cel. POKROWSKI and his deputy Lt. Col. SORKIN.	25
	section were: Col. Portowall and the deputy and had no encedalized	
	POKROWSKI was a delonel-engineer, but had no specialized	25
	knewledge of mathematics or ballistics. SORKIN on the other hand was	
	trained in ballistics, and had also occupied himself with rocket	
	he warked at that time on questions or	25
	the mechanics and dynamics of hadies with variable mass. Except for	
	these two. no other Soviets had contact with the section led by Prof.	
	KLOSE.	25

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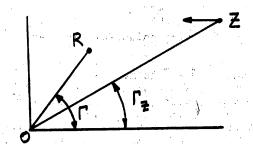
The task for the KLOSE group was the re-designing of the development of the AA-rocket "Wasserfall". The work was mainly in calculations. the KLOSE group had been working on this task for several menths. The reference data available to the KLOSE group was very scarce. Several design drawings of the whole worket were available, but they contradicted each other in detail. KLOSE intended to attend to the ballistic problems himself, STANGE to the

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RLOSE group. Especially unclear at that time was the problem of the guidance of the missile. Only several weeks after my arrival did SORKIN appear with an equation, which was given the designation: "differential equation of the ground calculating machine of the rocket 'Wasserfall'" - the applicable figure is shown below.

seredynamic questions, and KLUGH to the thermodynamic problems.



P - mooket

Z = target

0 = launching point assumed identical with the ground station

- angle of elevation, at which the recket appears from the ground station, \(\sum_{\text{z}} \) corresponding angle for the target (aircraft)

Figure #4

51. The equation was a differential equation of second order for Γ which connects Γ with Γz. The exact form of the equation is no longer known to me. The following values appeared in the equation:

of $\lceil - \rceil_2$ a function of $\lceil - \rceil_2$ and a function of t. The function of $\lceil - \rceil_2$ had the form, when $\lceil - \rceil_2 = S: \Re(S) = \frac{AS}{1 + bS + CS^2}$ or similar, with constant values for a, b, c. This was valid when S was not too great. For $S = 30^\circ$, g(S) was constant equal 3.9 e/sec (?) the function of t was: $f(t) = \frac{12}{(t-S)}$

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should be calculated until the impact of the rocket on the the target-seeking procedure.

- Thus, the flight path of the recket consisted of three parts: (1)
 a vertical ascent in the first six seconds after the launching; (2)
 the arc of deflection determined by the calculating unit; and (3) the
 target seeking path. When the target approach lay in a vertical plane
 through the launching point, then the differential equation of the palculating unit is sufficient for determining the movement of the rocket.

 In any other movement of the target, further data is needed; for example,
 the side angle against a fixed direction in the horizontal plane,
 perhaps the x direction. We information at all could be gained in
 this respect, neither at Gema in Berlin, nor later in the USSR. Other
 German working groups at Gema, which possibly had some knowledge about
 the calculating unit were not asked about this by KLOSE. SORKIN, who
 had given us the differential equation, could not say anything more.

 not told about the make-up or the operation of the calculating
 unit. Thus, one of the most important questions, namely under what
 command the rocket should fly in space, remained unsolved. Consequently, worked in Berlin enly with plane trajectories of the
 rocket "Wasserfall".
- 54. But several weeks passed before trajectory investigations for "Wasserfall" could start at all. began only in the second 25X1 half of September 1946 with a trajectory calculation. Until then, even preliminary data on weights, thrust, weight rate of flew, gas exhaust velocity, etc., were missing.

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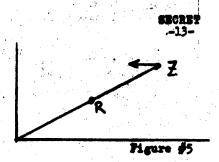
- 55. During the first part of __work_at Gema, weights and center of gravity location were calculated from eld designs. STANGE occupied himself with the theoretical determination of resistance and lift factors and the shift of center of pressure. KLUGE made theoretical examinations of the exhaust velocity of the combustion gases and of the thrust.
- 56. In the ballistic field, several general examinations were started at this time. Several target tracking procedures for antigiroraft rockets were examined:

the first of the second of the

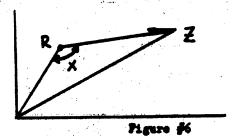
a. The target seeking method. The rocket is guided from a ground station in such a way, that ground station O, rocket R and target Z are always on one line (see Figure No. 5).

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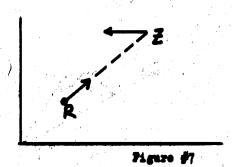




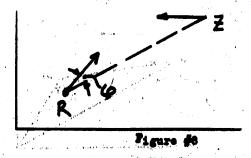
b. Generalisation. The rocket is guided from the ground station in such a way that the angle between ground station, rocket, and target has a fixed value x (see Figure #6).



c. Dog curve. The rechet has a searcher head, and flew in such a way that its longitudinal axis always aims at the target. In mathematical calculations, the condition was also accepted that the trajectory tangent always points at the target (see Figure #7).



d. Dog curve with angle of lead. The rocket flies in such a way that its longitudinal axis (or the trajectory tangent) always forms a prescribed angle (angle of lead) with the connecting line from rocket to target (see Figure #6).



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57. For x = 180°, case b.. above, becomes a.; for x = 0°, case d. becomes c. In these tasks the equations for the trajectory calculations were first formulated, and secondly the transverse accelerations appearing in each procedure were examined.

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8. Prof. KLOSE made stability examinations for the first part of a vertical ascent after the start and used thus already provisional data for the "Wasserfall".

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Data for "Wasserfall"

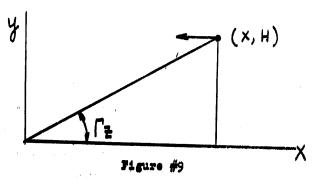
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- O. The starting weight was about 3.8 tons, the thrust on the ground 8 to 8.3 tons, the burning period 46 seconds. The jet rudders were dropped off in the seventeenth or nineteenth second.
 - The c values in the subsonic region (Ma < 0.8) for $\alpha = 0$ were approximately c = 0.250, the maximum of c (under Ma = 1.1 to 1.2) was 0.8 or more.

Mo tion Equations for a Plane Al Rocket Trajectory

First the motion of the target is given. In the most simple case the aircraft flies in a vertical plane through the launching point of the rocket (x,y-plane), in constant altitude H with constant velocity V and in the direction of the negative x-axis (abscissa of the target equals X).



63. Then the cotangent of the angle of elevation is a linear function of the time:

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- 64. Therefore \(\bar{\gamma} \) and the time derivatives are known, and it is possible to calculate the angle of elevation \(\bar{\gamma} \) of the rocket and its derivatives from the differential equation of the calculating unit (or from \(\bar{\gamma} \) if the rocket flies with the target-seeking method. The starting conditions are \(\bar{\gamma} = \begin{align*} 20^{\circ}, \bar{\gamma} = 0 \\ \text{for } t = 6 \text{ sec. } \(\bar{\gamma}, \bar{\gamma} \) can therefore be regarded as given. For the treatment of the motion equations (1), etc. it is evident to use polar coordinates
 - (12) X= r cosp
 - (13) Y= r sin P

Differentiation results:

- (14) x= r cost r r sin F
- (15) = r sinf + rf cosf

It follows:

- (16) V2= ×2+ ×2 = +2++2 +2
- (17) ٧٧= ゲナナナ (ゲナナゲ)

If the first force equation is multiplied with v, then there follows:

v. can hereby be expressed by (16) by the polar coordinates and their derivatives. The same hold for V(n) based on the equations (9) and (15).

- (19) Vsing= rsin [+rf cos [
- 66. The right side of (18) also depends upon the altitude (because of 8, W, g). It is possible to take y for the altitude in case of AA rockets with little distances from the launching point, which can be reduced by (15) to r and Γ . There with (18) represents a differential equation of second order for r, and r is the only unknown. (Y is at the beginning of the calculation different from sere, since the starting values are the values for t = 6 sec in the vertical ascent.)
- 67. By calculating r through integration of (18), v is also given through (16) and y through (15). The abscissa x is found through (12) and the trajectory angle of inclination (can finally be determined through (19).
- 68. Appropriate formulas for calculation of the trajectory angle of inclination (can also be found in another ways

Differentiation results in

. .

M.A.

By consideration of (8), (9), (12), and (13) follows: $V(\cos \sin \Gamma - \sin \alpha \cos \Gamma) + \Gamma r(\cos^2 \Gamma + \sin^2 \Gamma) = 0$ or (20) $V \sin (\alpha - \Gamma) = r \Gamma$

Correspondingly follows from X Cosp + y Sinp = Y through differentiation

(21) V cos (8-1) = +

From (20) and (21) follows by division

(22) tan (r-1) = rr

69. Each of the formulas (19), (20), (21), (22) can be used for the calculation of . In the second force equation appears the derivative , which is found through differentiation of one of the formulas (19) to (22); for example from the formula (20):

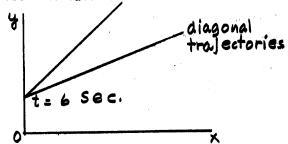
or on account of (20) and (21):

This is an exact formula for the transverse acceleration.

70. Angle of incidence and rudder angle are to be calculated by the equations (4) to (7).

"Wasserfall" Calculations at Gema (until 22 October 1946)

- 71. When approximate preliminary data for weight, thrust and resistance coefficients were known, several vertical ascents were calculated, based on different values for starting weight and starting thrust.
- 72. Furthermore, linear inclined trajectories with starting values for t = 6 sec were calculated.



- 73. Since lift coefficients were known and the function of the resistance coefficients with the angle of attack and the rudder angle were determined, the influence of the o increase on the burning cut-off speed and the burning cut-off location was examined. The dependence of the o value on and M was formulated;

 CW CW, + CW X + CW M2 + C(3) & M.

 This equation had been used previously in Gema.
- 74. The increase of the C -value by considering the dependency on and Y was very substantial, even if the beginning of the transverse trajectory was neglected. The beginning of the transverse trajectory demands by comparison with normal trajectories with slow deflection from the vertical ascent; very great angles of incidence.

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The result wass in transverse trajectories the air resistance becomes so much greater, that the gain on cut-off velocity by the more favorable weight component Mg Sin & , in comparison to the vertical ascent, is lest again. This result was later confirmed by more accurate trajectory calculations 25X1 in the USSR.

- In steep and also in level trajectories the cut-off velocity was about 800 m/sec er slightly more. The consideration of the strong dependency of the c value on & and ? produced the result that the equations (4) and (6) had to be solved simultaneously with the equation (18).
- 77. The differential equation of the calculating unit was examined, to determine when the deflection arc is completed and the target appreach begins. The result is that the point of time can be rather late in seme approaches (\approaches 38 sec.). The target approach path would in such a case only begin in rather high altitude (8 to 9 kilometers) and a target which flies at low altitude could not be attacked with the rocket "Wasserfall" for such an approach.
- 78. In the second half of September 1946 a trajectory calculation was done by utilizing the differential equation of the calculating unit according to the above described constians

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- 79. In the first half of October 1946 SORKIN asked Prof. KLOSE to make reports on the current research. This was done saw these reports 25X1 again in the spring of 1947 in Ostashkov. They were compiled in three volumes with the following titles:
 - Institute Berlin: Ballistics of the Rocket Wasserfall.
 - Institute Berlins Aerodynamics of the Rocket Wasserfall.
 - Institute Berlins Thermodynamics of the Rocket Wasserfall.

The first volume contained Prof. KLOSE's and examinations, the second contained STANGE's examinations and also design data, the third was the work of KLUGE.

On the 22nd of October Prof. KLOSE sent to the USSR. The remainder of the co-workers of KLOSE's group remained in Germany and were, shortly after departure, given notice at Gena. STANGE, and 25X1 perhaps a few others, were then still working for a short time closing the office. Meither STANGE nor KLUGE went to the USSR.

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